

# Distributed Neighbor Discovery in Ad Hoc Networks Using Directional Antennas

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# Motivation

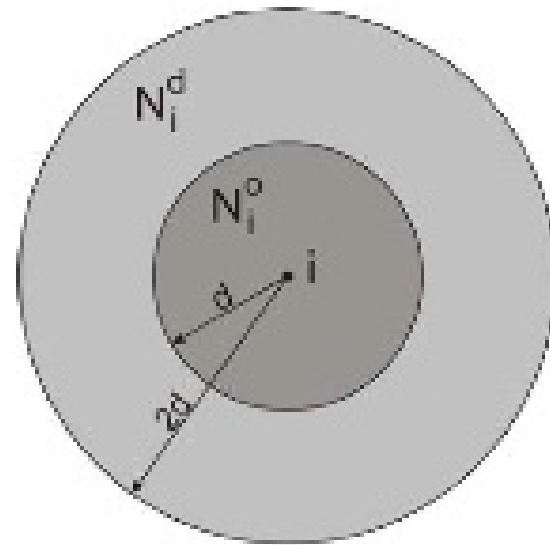
- Design algorithm for neighbor discovery in ad-hoc network
  - Directional antennas
  - Distributed algorithm
- Minimize number of neighbors involved in the discovery process
- Maximize number of one hop neighbors discovered



# Directional vs. Omnidirectional antennas

## Directional:

- Minimizes interference
- Transmission range extended
  - Assume range twice the size
- More nodes can be reached in one hop



$$N_i = N_i^d + N_i^o$$

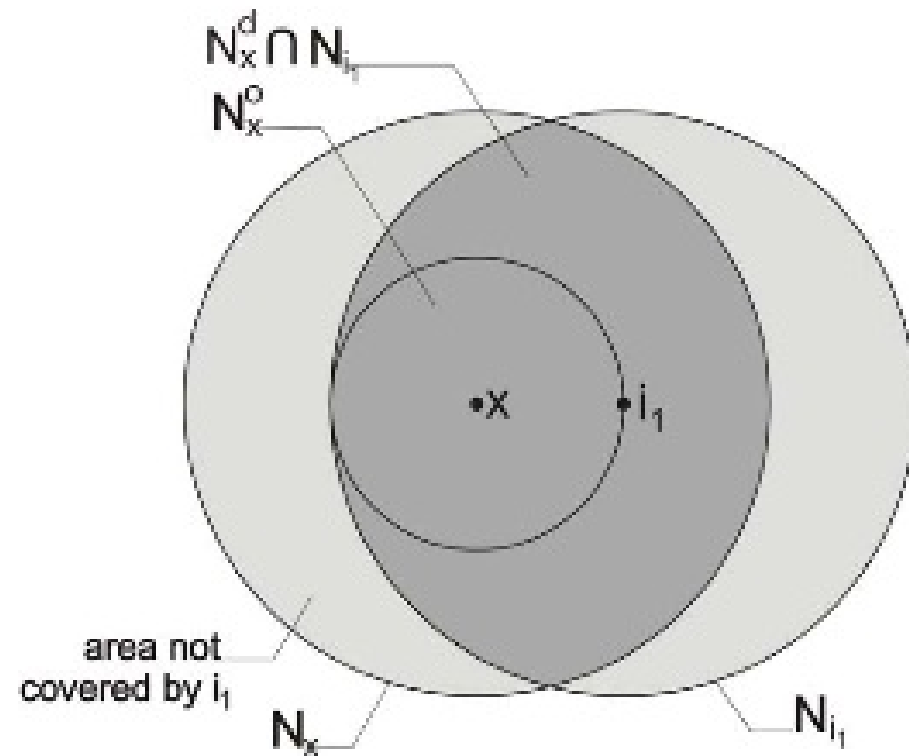
**Figure 1. Sets of neighbors of node  $i$ .**

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## Algorithm 1 Node $x$ joining the system

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- 1: Let  $N_x$  be the neighbor list of node  $x$   
 $N_x \leftarrow \emptyset$
  - 2: broadcast request message using omnidirectional transmission to initiate neighbor discovery process
  - 3: wait for response messages containing neighbor information from the representative nodes
  - 4: **for all** neighbor information  $R$  contained in the received response messages **do**
  - 5:      $N_x \leftarrow N_x \cup R$
  - 6: **end for**
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**Figure 2. Worst case scenario in choosing the first representative node,  $i_1$ .**



# Representative Nodes

The nodes included in set  $S$  should be chosen such that

- the union of the directional transmission range  $2d$  of all nodes in  $S$  covers the directional transmission range  $2d$  of node  $x$ , i.e.

$$N_x \subset \bigcup_{i \in S} N_i$$

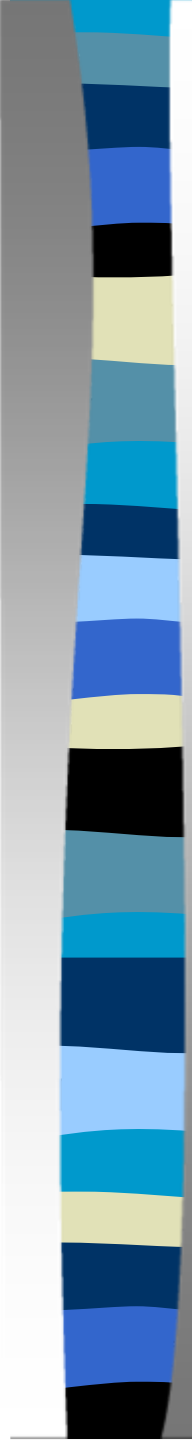
- the number of nodes in  $S$  is minimized.

Intuitively, the best case for the number of nodes in  $S$  is 1, i.e. when the representative node is located extremely close to  $x$ .



# Representative Node Heuristic

- Select node closest to  $x$
- If there is a tie, select first node in cw direction starting north of  $x$
- Repeat selection till there are no new neighbors to be added
- This heuristic guarantees to cover 68.4% of directional area



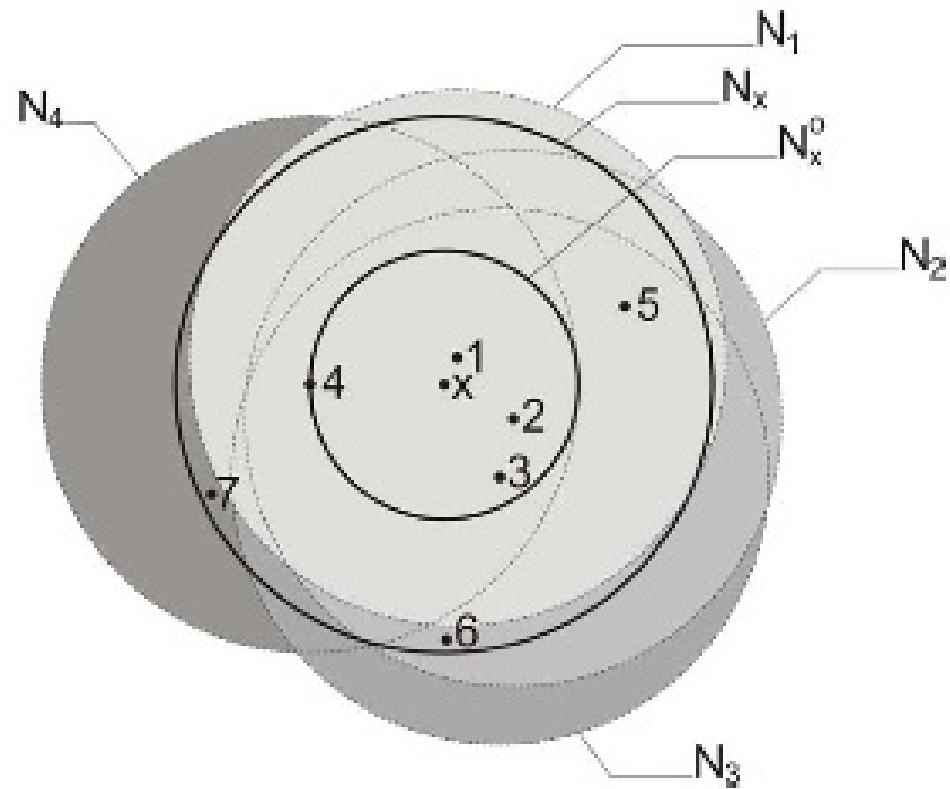
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**Algorithm 2** Each node  $i$  in the omnidirectional transmission range of  $x$

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1: receive broadcast request message from  $x$ 
2: Let  $N_i$  be the neighbor list of node  $i$ 
    $N_i \leftarrow N_i \cup \{x\}$ 
3:  $W \leftarrow (N_i \cup \{i\}) - \{x\}$ 
4: for all  $j \in W$  do
5:   if  $distance(x, j) > 2d$  then
6:      $W \leftarrow W - \{j\}$ 
7:   end if
8: end for
9:  $Z \leftarrow W$ 
10: sort all  $j \in W$  in ascending order based on  $distance(x, j)$ , then
    based on  $angle(x, j)$ 
11: for all  $j \in W$  do
12:   if  $j = i$  then
13:     exit for
14:   end if
15:    $Z \leftarrow Z - \{j\}$ 
16:   for all  $k \in W, k \neq j$  do
17:     if  $distance(j, k) \leq 2d$  then
18:        $Z \leftarrow Z - \{k\}$ 
19:     end if
20:   end for
21: end for
22: if  $Z \neq \emptyset$  then
23:   send  $Z$  to  $x$  using directional transmission
24: else
25:   do nothing
26: end if
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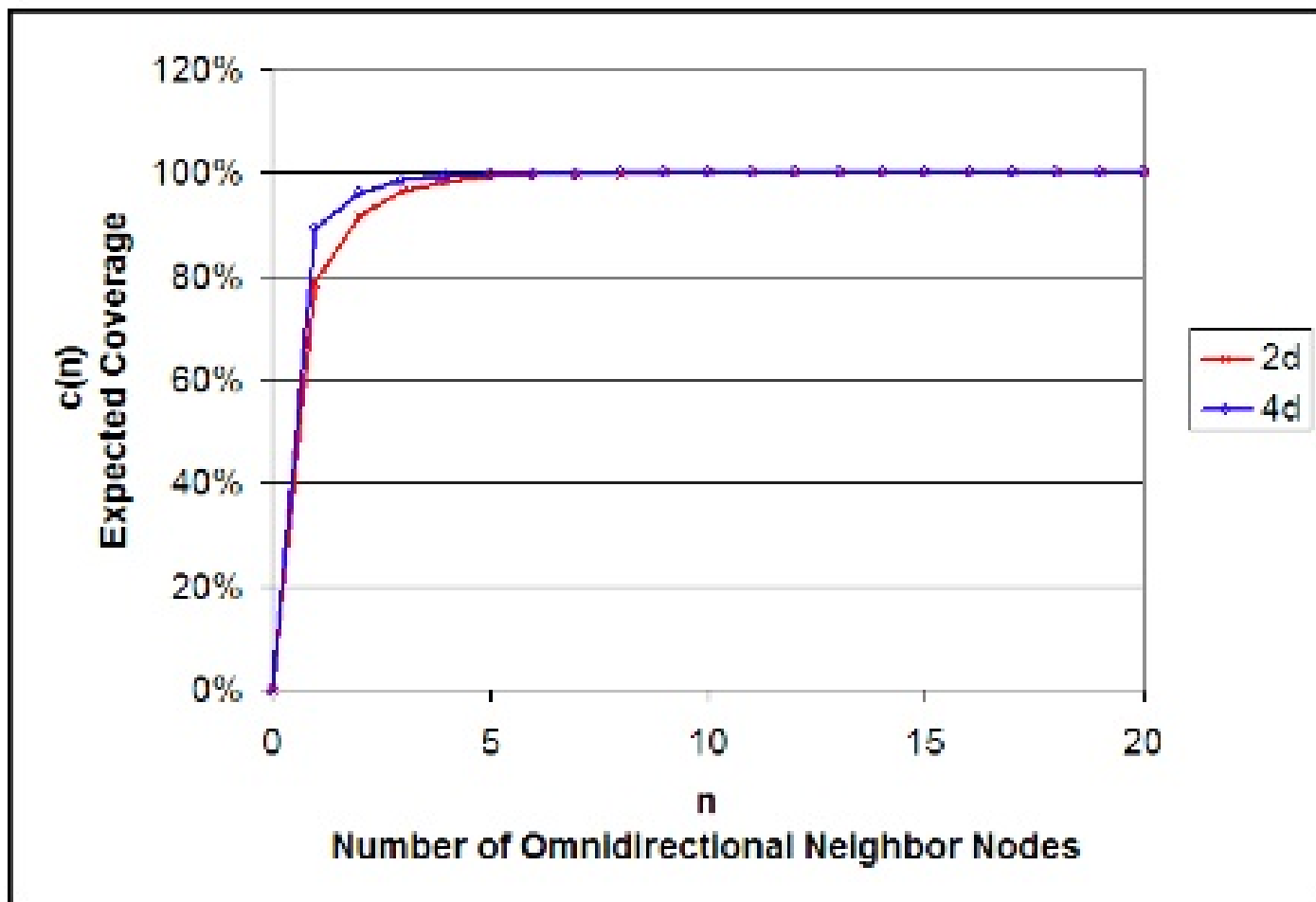


**Figure 3. Scenario of a new node  $x$  starting the neighbor discovery process.**



# Analysis

- Number of new neighbors discovered depends on the number and position of neighbors in the omnidirectional area
- Use Monte Carlo technique to calculate  $C(n)$  - Expected coverage



**Figure 4. Expected coverage  $c(n)$  against the number of neighbor nodes inside the omnidirectional transmission range.**



# Expected coverage

- Omnidirectional range

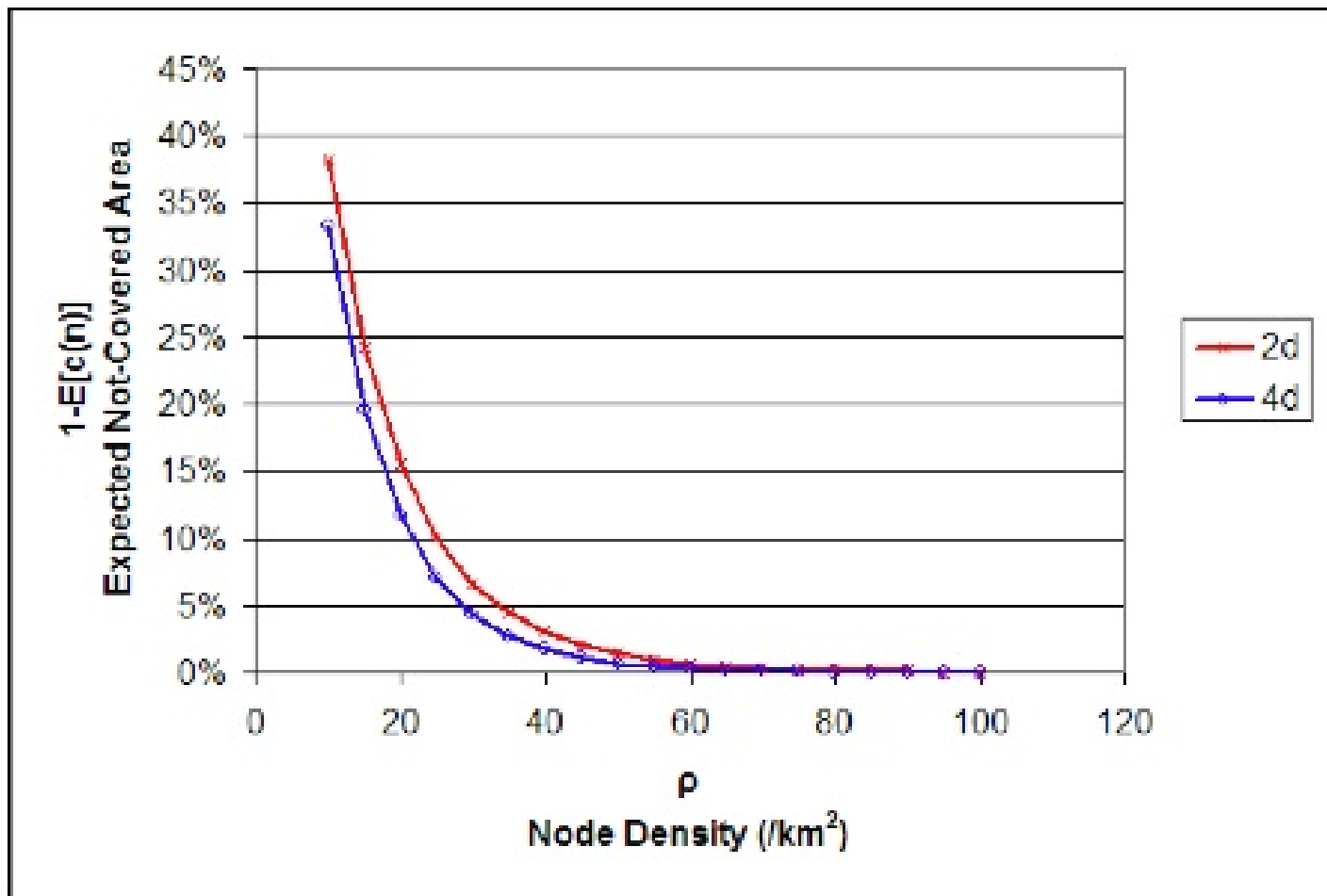
$$\lambda = \rho \pi d^2$$

- Probability finding  $n$  nodes in omnidirectional area

$$p(n) = \frac{\lambda^n e^{-\lambda}}{n!}$$

- Expected coverage

$$E[c(n)] = \sum_{k=0}^{\infty} p(k)c(k)$$

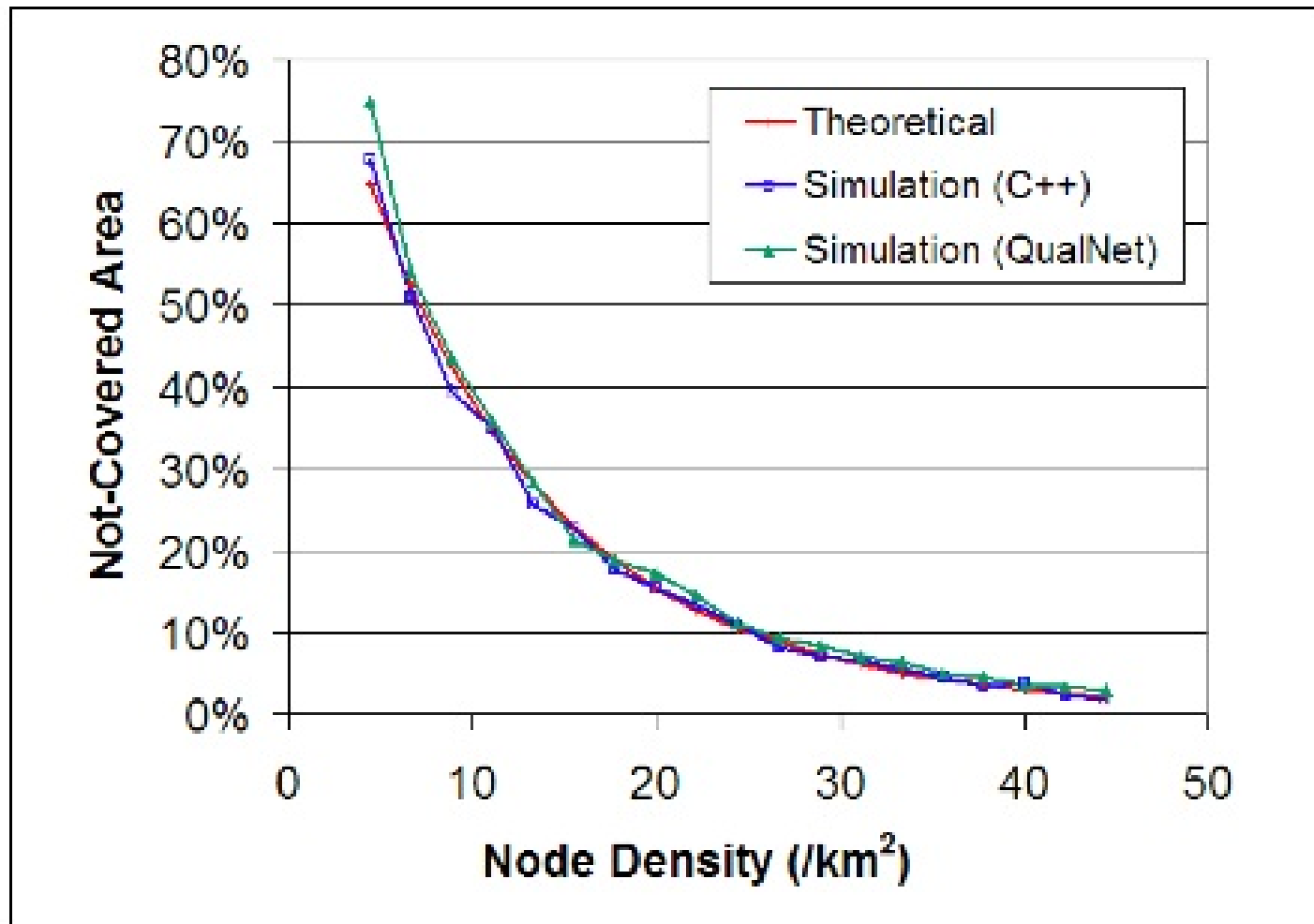


**Figure 5. Expected area not covered by the proposed neighbor discovery algorithm against the node density.**

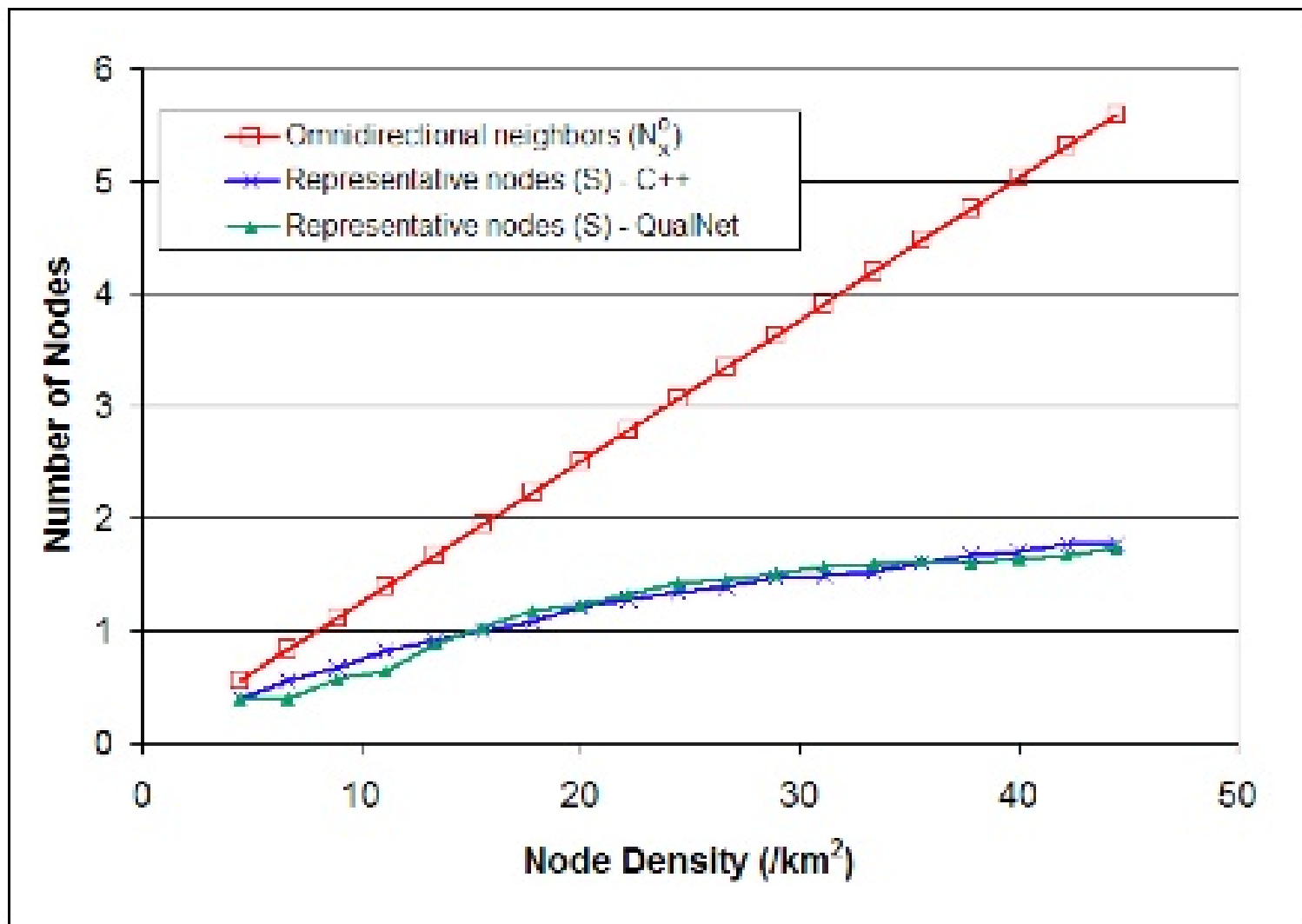


# Simulation

- Randomly scattered  $n$  nodes
- 1500x1500 meters
- Uniform distribution
- Omnidirectional range 200m
- Directional range 400m



**Figure 6. Actual not-covered area obtained from the simulation vs expected theoretical not-covered area.**



**Figure 7. Average number of representative nodes against the node density.**